

The Modern Environmental Macroeconomics

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Modelling the Climate after the Industrial Revolution-1

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- Approximately one-third of this is directly reflected back to space.
- In equilibrium, the resulting net short-wave radiation must be balanced by the outgoing long-wave radiation.
- At a pre-industrial equilibrium state the incoming and outgoing energy fluxes were equal, and the global mean temperature was therefore constant on the average.

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- Because of the perturbation, the incoming energy flux is larger than the outgoing flux, which leads to increasing temperature.

Modelling the Climate after the Industrial Revolution-3

- Under a perturbation $F(t)$ the evolution of global mean temperature can be described by

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- The parameter σ determines how quickly the temperature changes due to a given imbalance in the fluxes.

Modelling the Climate after the Industrial Revolution-4

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- Since the outflow of energy has a larger content of infrared radiation than does the inflow, an increase in the concentration of these gases has a strong positive effect on the energy balance.
- That is, it generates a positive forcing F .
- Gases with this property are called greenhouse gases (GHGs). Even a small concentration of such gases has a large effect on the energy balance of the earth.

- Carbon dioxide is the most important of these gases and its effect on the energy balance is approximated by the "Arrhenius (1897) formula":

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Modelling the Climate after the Industrial Revolution-5

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- where $S(t)$ and S_0 represent the current and preindustrial atmospheric CO_2 concentrations, respectively.

Modelling the Climate after the Industrial Revolution-6

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Modelling the Climate after the Industrial Revolution-6

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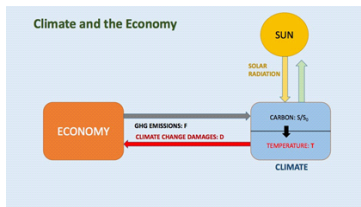
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- The coefficient $\lambda = \frac{\eta}{\kappa - \zeta}$ is called the equilibrium climate sensitivity and captures the response in the global mean temperature to a doubling of the CO₂.

Modelling the Climate after the Industrial Revolution-7

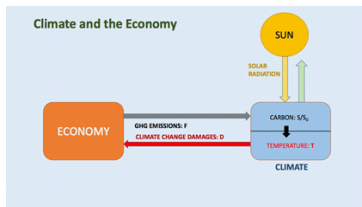
The link with the Economy-1



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Modelling the Climate after the Industrial Revolution-7

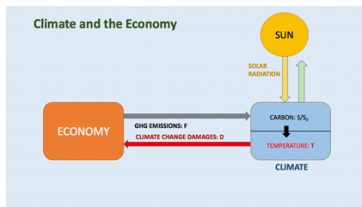
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Modelling the Climate after the Industrial Revolution-7

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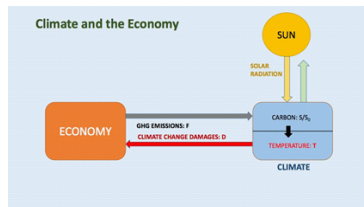


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- GHG emissions E increase the actual atmospheric CO_2 (or GHGs) concentration relative to preindustrial levels

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- where d_{t-s} is the carbon depreciation function.

Modelling the Climate after the Industrial Revolution-8

The link with the Economy-2

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- **the remainder decays with a half-life of a few centuries**

Modelling the Climate after the Industrial Revolution-9

Climate-Economy Dynamics

- The coupled dynamic system describing climate and the impact of the economy, that is the impact from GHG emissions on temperature, is given, in continuous time by:

$$\dot{T}(t) = \frac{\gamma}{\ln 2} \ln \left(\frac{S}{S_0} \right) + F_{EX} + \delta T(t)$$

$\delta = \zeta - \kappa$, $\gamma = \sigma\eta$, F_{EX} : exogenous forcing

$$\dot{S}(t) = E(t) - dS(t), \quad S(t) = S_0$$

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- The coupled dynamics can be expanded by introducing the ocean temperature and taking into account that atmospheric temperature increases much faster than the oceans.

- Emissions can be expressed as a by product of output, that is:

$$E(t) = g(Y(t)), Y(t) = f(K, L)$$

$$E(t) = s(t) [A(t)K(t)^\alpha L(t)^{1-\alpha}]$$

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- or can be regarded as an input in the production function representing the use of fossil fuels:

$$Y(t) = f(K, L, E)$$

$$Y(t) = A(t)K(t)^\alpha L(t)^\beta E(t)^{1-\alpha-\beta}$$

Modelling the Climate after the Industrial Revolution-11

Emissions vs Temperature: A Linear Relationship-1

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- The constant of proportionality is called the transient carbon response parameter (TCRE). This parameter is defined as the ratio of temperature change to cumulative carbon emissions, and it is approximately independent of both the atmospheric CO₂ concentration and its rate of change over different time scales.

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- The constant of proportionality is called the transient carbon response parameter (TCRE). This parameter is defined as the ratio of temperature change to cumulative carbon emissions, and it is approximately independent of both the atmospheric CO₂ concentration and its rate of change over different time scales.
- The TCRE is estimated to be in the range of 1.3 – 2.1°C per trillion tones of carbon (TtC) [or per 1000 PgC] emitted).

Modelling the Climate after the Industrial Revolution-12

Emissions vs Temperature: A Linear Relationship-2

- The linear model has been derived and verified over the relevant range of emissions by MacDougall and Friedlingstein (2015) with the TCRE defined as:

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Modelling the Climate after the Industrial Revolution-12

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- where, $\Delta T(t)$ is change in global average temperature up to time t ; and $CE(t)$ are cumulative carbon emissions up to time t .

Modelling the Climate after the Industrial Revolution-13

Emissions vs Temperature: A Linear Relationship-3

- In the context of the near proportional relationship between $CE(t)$ and $\Delta T(t)$, the anthropogenic impact on the global temperature increase can be approximated in continuous time by

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- where, $CE(t) = \int_{s=0}^{\infty} E(s) ds$ denotes cumulative global carbon emissions up to time t and Λ is the TCRE. Taking the time derivative of this expression, we obtain

$$\dot{T}(t) = \Lambda E(t), \quad \Lambda = 1.7 \pm 0.4^{\circ}\text{C per TtC}$$

Modelling the Climate after the Industrial Revolution-14

Emissions vs Temperature: A Linear Relationship-4

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Emissions vs Temperature: A Linear Relationship-4

- This linear relationship provides a simplification of climate models and the current research on the economics of climate change has started using it.
- After the presentation of the basic mechanism driving the global mean temperature and the basic links with the economy, we proceed to present the coupled economy-climate models which are used for policy design, and to provide the modern approach to the study of macroeconomic policy under conditions of climate change.